## Influence of proximity effect with Umklapp processes on the Josephson current in the SFS nanostructure

Yu. Proshin and V. Tumanov

Institute of Physics, Kazan University, Kazan, Russian Federation

We consider the Josephson effect in symmetric superconductor-ferromagnetic-superconductor (SFS) system. The Josephson current is calculated as a function of the ferromagnetic layer thickness  $d_f$ . The Fulde-Ferrell-Larkin-Ovchinnikov (FFLO) pairs in the F layer have a nonzero wave vector, and the transformation the BCS pairs to the FFLO pairs (and vice versa) at passing through SF (FS) borders may be proceeded through the Umklapp processes<sup>1</sup>. To estimate the influence of proximity effect we use the expansion of superconductor energy in the powers of an order parameter (near the critical temperature  $T_c$ ). We take into account the dependence of the critical temperature  $T_c$  from the phase difference  $\varphi$  between the order parameter in the left and right S side of the SFS contact, respectively, i.e.  $T_c = T_c(\varphi) = T_{c\varphi}$ . The result expression for critical current incorporates a term proportional to  $T_{c0} - T_{c\pi}$  which gives the main contribution near  $T_c$ . Our results are compared with known data for the NbCu<sub>0.47</sub>Ni<sub>0.53</sub>Nb nanostructures<sup>2</sup> where the critical Josephson current oscillations due to transitions between 0 and  $\pi$  phase state were observed. A good agreement is obtained by taking into account the Umklapp processes.

<sup>1</sup>Yu. A. Izyumov, Yu. N. Proshin, and M. G. Khusainov, Physics/Uspekhi **45**, 109 (2002). <sup>2</sup>V.V. Ryazanov et al., Rev. Low Temp. Phys. **136**, 385 (2004).